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# Compensation of $p$ -type doping in Al-doped 4H-SiC

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## ABSTRACT

One of the major challenges of 4H-silicon carbide (4H-SiC) is that the preparation of low resistivity  $p$ -type 4H-SiC single crystals lags seriously behind that of low resistivity  $n$ -type 4H-SiC single crystals, hindering the development of important 4H-SiC power devices such as  $n$ -channel insulated gate bipolar transistors. In particular, the resistivity of  $p$ -type 4H-SiC single crystals prepared through the physical vapor transport technique can only be lowered to around 100 m $\Omega$  cm. One of the key causes is the incomplete ionization of the  $p$ -type dopant Al with an ionization energy  $\sim 0.23$  eV. Another factor is the compensating effect. It cannot simply assume nitrogen (N) is the sole compensatory center, since the number of the compensating center is larger than the concentration of N doping. In this work, we systematically investigate the compensation of native defects and self-compensation in Al-doped 4H-SiC. It is found that the positively charged carbon vacancies ( $V_C^{2+}$ ) are also the dominant compensating centers in Al-doped 4H-SiC. When the Al concentration is in the range of  $10^{16}$ – $10^{19}$  cm $^{-3}$ , the concentration of holes is lower by one order of magnitude than the Al concentration because of the compensation of  $V_C^{2+}$ . As the Al concentration exceeds  $10^{20}$  cm $^{-3}$ , the concentration of holes is only in the order of magnitude of  $10^{19}$  cm $^{-3}$  owing to the dominant compensation of  $V_C^{2+}$  and supplementary self-compensation of interstitial Al ( $Al_i^{3+}$ ). We propose that the passivation of  $V_C^{2+}$  as well as quenching is effective to enhance the hole concentration of Al-doped 4H-SiC.

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## I. INTRODUCTION

With the rapid development of power electronics, 4H-silicon carbide (4H-SiC) has been attracting great attention owing to its unique physical properties such as wide bandgap, high breakdown electric field strength, and high thermal conductivity.<sup>1–3</sup> Compared with traditional Si power devices, 4H-SiC power devices such as Schottky barrier diodes (SBDs) and metal-oxide-semiconductor field effect transistors (MOSFETs) possess advantages of higher frequency, higher power-conversion efficiency, lower power loss, and smaller size.<sup>4–10</sup> More significantly, 4H-SiC-based bipolar devices such as gate turn-off thyristors (GTOs) and insulated gate bipolar transistors (IGBTs) hold great promise for ultrahigh voltage

(>10 kV) applications, which exceed the working scope of Si-based power devices.<sup>10–15</sup> Current GTOs and IGBTs are fabricated on  $n$ -type 4H-SiC substrates with very low resistivity, which lead to  $p$ -channel devices. Since the mobility of electrons is much higher than that of holes in 4H-SiC,  $n$ -channel power devices may have better performance than  $p$ -channel power devices.<sup>14,15</sup> However, the development of  $n$ -channel IGBT has significantly lagged behind that of  $p$ -channel power devices because it is rather difficult to obtain  $p$ -type 4H-SiC substrates with very low resistivity. At present, researchers have developed an inverted-growth process that, in principle, could allow all critical epilayers ( $p$ -type 4H-SiC) to be grown in a continuous sequence on an original  $n$ -type substrate ( $\sim 400$   $\mu$ m), which is subsequently removed by polishing.<sup>15</sup> A  $p$ -type 4H-SiC

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substrates with very low resistivity will be helpful for researchers to fabricate  $n$ -channel power devices in a direct-growth process.

Until now, the resistivity of  $p$ -type 4H-SiC single crystals with low resistivity that are still in the research stage has not been reduced below 30 m $\Omega$  cm.<sup>16–22</sup> In particular, the resistivity of  $p$ -type 4H-SiC single crystals prepared via the (physical vapor transport) PVT method can only be reduced to about 100 m $\Omega$  cm.<sup>19–22</sup> One of the major reasons is the incomplete ionization of the  $p$ -type dopant Al. Among all group-III elements, Al has been found to be the best  $p$ -type dopant in 4H-SiC, but the ionization energy of Al in 4H-SiC is still high,  $\sim 0.23$  eV, which leads to the acceptor's ionization rate only about 5%–30% at room temperature.<sup>23,24</sup> Another reason is the compensation effect.<sup>25–30</sup> Presently, it is commonly assumed that nitrogen (N) is the principal compensating center.<sup>25,26</sup> Several experiments, however, indicate there is an additional compensating center in  $p$ -type SiC because the number of the compensating center is more than the concentration of N doping. Krieger *et al.* grew a bulk crystal of 6H-SiC using PVT with an Al doping concentration of  $\sim 1.6 \times 10^{19}$  cm $^{-3}$ . The concentration of the compensating center is  $4.0 \times 10^{18}$  cm $^{-3}$  identified by the Hall effect measurements, which is higher than the N doping concentration ( $3.0 \times 10^{18}$  cm $^{-3}$ ) measured by secondary ion mass spectroscopy (SIMS).<sup>25</sup> A similar phenomenon is seen in Al-doped  $p$ -type 4H-SiC epilayers synthesized through chemical vapor deposition (CVD). Asada *et al.* grew Al-doped  $p$ -type 4H-SiC epilayers with a density of acceptors of about  $7.1 \times 10^{18}$  cm $^{-3}$  and a compensating center density of approximately  $1.2 \times 10^{16}$  cm $^{-3}$ . SIMS measurements indicate that the N doping concentration is less than  $5.0 \times 10^{15}$  cm $^{-3}$ , which is an order of magnitude less than the compensating center.<sup>27</sup> All of these experiments suggest the existence of an additional compensating center, but the mechanism by which this compensation occurs remains unclear. Carbon vacancies ( $V_C$ ) and  $V_C$ -related defects are widely considered to be the principal compensating center in Al implanted  $p$ -type SiC.<sup>28–30</sup> This is because co-implanting Al and C may enhance the concentration of free holes by a factor of 1.5–2.5.<sup>28</sup> At the moment, it is unknown if  $V_C$  serves as a compensating center for the as-grown Al-doped  $p$ -type SiC.

In this work, we systemically investigate the compensation mechanisms of  $p$ -type doping in as-grown Al-doped 4H-SiC. The compensation of native defects and the self-compensation of interstitial Al ( $Al_i$ ) are revealed in the framework of first-principles calculations. It is found that the positively charged carbon vacancies ( $V_C^{2+}$ ) are the dominant compensating centers in Al-doped 4H-SiC. When the Al concentration is in the range of  $10^{16}$ – $10^{19}$  cm $^{-3}$ , the concentration of holes is lower by one order of magnitude than the Al concentration because of the compensation of  $V_C^{2+}$ . As the Al concentration exceeds  $10^{20}$  cm $^{-3}$ , the concentration of holes is only in the order of magnitude of  $10^{19}$  cm $^{-3}$  owing to the dominant compensation of  $V_C^{2+}$  and supplementary self-compensation of interstitial  $Al_i^{3+}$ . The hole concentration of Al in 4H-SiC substrate and epilayer can be significantly improved with the passivation of  $V_C^{2+}$  and quenching.

## II. COMPUTATIONAL METHODS

### A. First-principles calculations

First-principles calculations are performed using the projector-augmented wave (PAW) method implanted in the Vienna *ab initio*

Simulation Package (VASP). The wave functions are expanded by using the plane wave energy cutoff of 500 eV. The Perdew–Burke–Ernzerhof (PBE) functional with the generalized gradient approximation (GGA) exchange correlation is employed to describe the exchange–correlation interactions.<sup>31</sup> Brillouin-zone integrations are approximated by using special  $k$ -point sampling of the Monkhorst–Pack scheme with a  $k$ -point mesh of  $2 \times 2 \times 2$ . The supercell lattice and atomic coordinates are fully relaxed until the total energy per cell and the force on each atom are less than  $1.0 \times 10^{-6}$  eV and 0.01 eV/Å, respectively. The screened hybrid density functional of Heyd, Scuseria, and Ernzerhof (HSE06) is adopted to calculate the electronic properties of 4H-SiC. Defects are modeled in a  $6 \times 6 \times 2$  supercell of 4H-SiC with 576 atoms. The calculated lattice parameters of 4H-SiC are  $a = 3.07$  Å and  $c = 10.05$  Å. The calculated bandgap energy of 4H-SiC is 3.18 eV, which agrees well with experimental results.<sup>1</sup>

### B. Defect formation calculations

The formation energy of a defect  $\alpha$  at the charge state  $q$  in 4H-SiC is calculated by using<sup>32,33</sup>

$$\Delta H_f(\alpha, q) = \Delta E(\alpha, q) + \sum n_i \mu_i + qE_F, \quad (1)$$

where  $\Delta E(\alpha, q) = E(\alpha, q) - E(\text{SiC}) + \sum n_i E(i) + qE_{VBM}$ , where  $E(\alpha, q)$  is the total energy of the SiC supercell containing the defect  $\alpha$  at the charge state  $q$ ,  $E(\text{SiC})$  is the total energy of the SiC supercell,  $E_F$  is the Fermi energy referred the valence band maximum (VBM) of SiC,  $n_i$  is the number of atoms removed from or added into the supercell, and  $\mu_i$  is the chemical potential of constituent  $i$  referred to elemental solid or gas with energy  $E(i)$ . In the case of charged defects, a charge correction to the formation energies is applied.<sup>34</sup>

Thermal-equilibrium conditions exert a series of thermodynamic limits on the achievable values of  $\mu_i$ . First, the values of  $\mu_i$  are limited to those values that maintain stable SiC,

$$\mu_{\text{Si}} + \mu_{\text{C}} = \Delta H_f(\text{SiC}). \quad (2)$$

Second, for the avoidance of the precipitation of Si, C, and Al, the values of  $\mu_i$  are limited by

$$\mu_{\text{Si}} \leq 0, \mu_{\text{C}} \leq 0, \mu_{\text{Al}} \leq 0. \quad (3)$$

Finally, for the avoidance of the formation of secondary phases of  $Al_4C_3$ , the values of  $\mu_i$  are limited by

$$4\mu_{\text{Al}} + 3\mu_{\text{C}} \leq \Delta H_f(\text{Al}_4\text{C}_3), \quad (4)$$

where  $\Delta H_f(\text{Al}_4\text{C}_3)$  is the formation energy of  $Al_4C_3$ . Solving Eqs. (2)–(4), we obtain the accessible range for the values of  $\mu_i$ , as shown by the green region in Fig. 1.

### C. Carrier density calculations

Based on the formation energies and the electronic structures of defects, we use the detailed balance theory<sup>26</sup> to calculate the Fermi energy and carrier concentration of Al-doped 4H-SiC. The

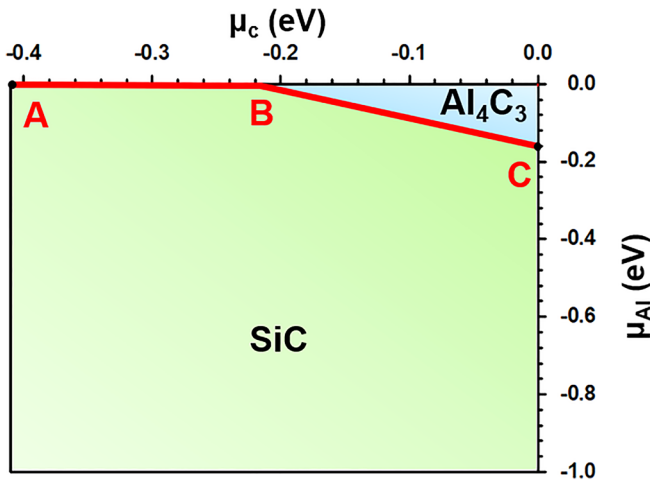


FIG. 1. Accessible range of chemical potentials (green region) for the thermal-equilibrium doping of Al in 4H-SiC.

concentrations of holes and electrons are calculated by using

$$p_0 = N_v e^{(E_v - E_F)/k_B T} = N_v e^{-E_F/k_B T}, \quad (5)$$

$$n_0 = N_c e^{-(E_c - E_F)/k_B T} = N_c e^{(E_F - E_g)/k_B T}, \quad (6)$$

where  $E_v$  and  $E_c$  are the energies of VBM and conduction-band minimum (CBM) of 4H-SiC, respectively.  $E_v$  are usually set to zero.  $E_g$  is the bandgap of SiC.  $k_B$  is the Boltzmann constant.  $N_v$  and  $N_c$  are the effective densities of states of the valence bands and conduction bands, respectively.  $N_v$  and  $N_c$  are given by

$$N_v = 2(2\pi m_p^* k_B T)^{3/2} / h^3, \quad (7)$$

$$N_c = 2(2\pi m_n^* k_B T)^{3/2} / h^3, \quad (8)$$

where  $m_p^*$  and  $m_n^*$  are the effective mass of holes ( $3.00 m_0$ ,  $m_0$  is the mass of free electron) and electrons ( $0.42 m_0$ ), respectively. The charge neutrality condition requires that

$$p_0 + n_D^+ = n_0 + n_A^-. \quad (9)$$

Here,  $n_D^+$  and  $n_A^-$  are the concentrations of positively charged donors and negatively charged acceptors, respectively. For ordinary doping conditions, the distribution of charged defects satisfies the Boltzmann distribution. For degenerate doping (i.e., the doping concentration exceeds  $N_v$ ), the distribution of charged defects satisfies the Fermi-Dirac distribution. Hence, the concentration for a defect  $\alpha$  with charge state  $q$  is calculated by the Boltzmann distribution or Fermi-Dirac distribution,

$$n(\alpha, q) = N_{site} g_q e^{-\Delta H_f(\alpha, q)/k_B T} \quad (\text{Boltzmann distribution}), \quad (10)$$

$$n(\alpha, q) = N_{site} \frac{1}{1 + \frac{1}{g_q} e^{-\Delta H_f(\alpha, q)/k_B T}} \quad (\text{Fermi-Dirac distribution}), \quad (11)$$

where  $N_{site}$  is the number of sites that may be occupied by the defect  $\alpha$  per volume and  $g_q$  is the degeneracy factor that corresponds to the number of possible electron configurations. For degenerate  $p$ -type 4H-SiC, we use the Pearson-Bardeen model<sup>1,17</sup> to make corrections on the ionization energy [ $\epsilon(0/-)$ ] of Al by  $\epsilon(0/-) = 0.23 - \alpha(N_{Al})^{1/3}$ , as shown in Fig. S1 in the supplementary material. In this case, the corrected formation energies of  $Al_{Si}^-$  are calculated by using

$$\begin{aligned} \Delta H_f(Al_{Si}^-) &= \Delta H_f(Al_{Si}^0) + \epsilon(0/-) - E_F \\ &= \Delta H_f(Al_{Si}^0) + 0.23 - \alpha(N_{Al})^{1/3} - E_F. \end{aligned} \quad (12)$$

Figure S2 in the supplementary material shows an example of the correction of  $\Delta H_f(Al_{Si}^-)$  of 4H-SiC with the Al concentration of  $2.0 \times 10^{20} \text{ cm}^{-3}$ . By solving Eqs. (1) and (5)–(12) self-consistently, we can obtain the carrier concentrations, Fermi energies, and defect concentrations of Al-doped 4H-SiC at a given temperature and chemical potential.

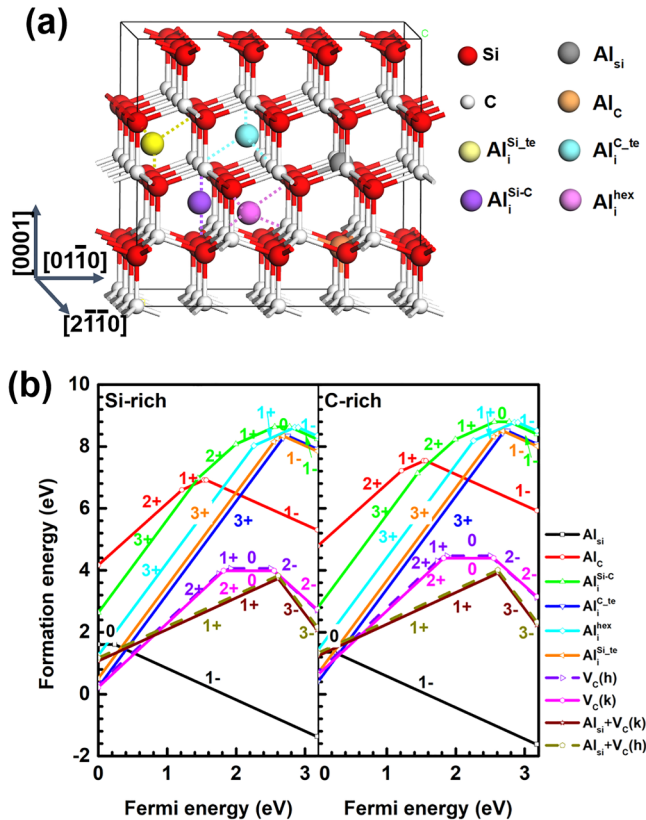
### III. RESULTS AND DISCUSSION

#### A. Formation energy

It is normally believed that Al is energy favorable located at the Si sublattice than the C sublattice. After substituting Si, it exhibits as an acceptor. However, whether it is energy favorable for Al located at the interstitial site is still unknown. Al at the interstitial site could be a potential compensating center. Moreover, the intrinsic defects in 4H-SiC also have the potential to compensate the holes. From the intrinsic defects, the carbon vacancy ( $V_C$ ) exhibits the negative-U behavior, which can be a donor for  $p$ -type 4H-SiC. For the interstitial defects, C interstitials ( $C_i$ ) and Si interstitials ( $Si_i$ ) are also donors. Among  $V_C$ ,  $C_i$ , and  $Si_i$ ,  $V_C$  has the lowest formation energy, and the formation energies of  $V_{Si}$ ,  $C_i$ , and  $Si_i$  are so large that their effects can be ignored. So,  $V_C$  has the biggest possibility to compensate Al-doped SiC. The interaction of  $V_C$  with aluminum acceptor is considered in this work. Gali *et al.*<sup>46</sup> show that  $V_C$  can be attached to the aluminum acceptor. The interaction of  $V_C$  with other defects is ignored. It has been reported that  $V_C$  can bind with  $V_{Si}$  or  $C_{Si}$  and form  $V_C-V_{Si}$  or  $V_C-C_{Si}$  complexes.<sup>35–37</sup> Compared with  $V_C$ , both  $V_C-V_{Si}$  and  $V_C-C_{Si}$  have much higher formation energy, which suggests that only a small part of  $V_C$  would form complexes.

As shown in Fig. 2(a), the defect configurations of Al in 4H-SiC considered in this work include interstitial Al ( $Al_i$ ), substitutional Al at C-lattice sites ( $Al_C$ ), and substitutional Al at Si lattice sites ( $Al_{Si}$ ). For  $Al_i$ , four types of interstitial sites are considered.  $Al_i^{C-te}$  and  $Al_i^{Si-te}$  are the Al atoms located at the carbon- and silicon-coordinated tetrahedral sites, respectively.  $Al_i^{Si-C}$  is the Al atom located at the hexagonal layer accommodating an equally carbon- and silicon-coordinated site.  $Al_i^{hex}$  is the Al atom located at

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**FIG. 2.** (a) Optimized atomic structures of different defect configurations of Al in 4H-SiC. Defect configurations of  $\text{Al}_C$ ,  $\text{Al}_{\text{Si}}$ ,  $\text{Al}_i^{\text{C-te}}$ ,  $\text{Al}_i^{\text{Si-te}}$ ,  $\text{Al}_i^{\text{Si-C}}$ , and  $\text{Al}_i^{\text{hex}}$  are denoted by gray, orange, cyan, purple, pink, and yellow balls, respectively. Host lattice sites of Si and C are denoted by red and white balls, respectively. (b) Calculated defect formation energies of Al,  $V_C$ , and  $\text{Al}_{\text{Si}}-V_C$  at the Si-rich limit and C-rich limit.

the site encompassed by the upper and lower hexagonal basal plane. We note that the nonequivalent sublattice sites of Si and C in 4H-SiC include the quasihexagonal (*h*) and quasicubic (*k*) sites. When constructing  $\text{Al}_C$  ( $\text{Al}_{\text{Si}}$ ), we substitute the lower-energy C (Si) at the *k*-site by Al.

The calculated formation energies of Al and  $V_C$  at the Si-rich limit (point A in Fig. 1) and the C-rich limit (point C in Fig. 1) are shown in Fig. 2(b). It is clear that substitutional Al in the Si lattice site is more energetically favorable than that in the C-lattice site. The calculated (0/−) transition energy of  $\text{Al}_{\text{Si}}$  is  $E_V + 0.23$  eV, which well agrees with experiment results.<sup>1</sup> Among all possible interstitial sites, the formation energies of  $\text{Al}_i^{\text{C-te}}$  are the lowest due to the steric effect. For *p*-type 4H-SiC, the 3+ charge state dominates the charge states of  $\text{Al}_i^{\text{C-te}}$ . It has been found that  $V_C$  is the dominant intrinsic defect in *p*-type 4H-SiC.<sup>38–44</sup> Therefore, we consider the compensation of  $V_C$  for the *p*-type doping of 4H-SiC.  $V_C$  acts as a negative-U center<sup>36</sup> in 4H-SiC. The (0/2−) transition levels of  $V_C(h)$  and  $V_C(k)$  are located at  $E_V + 2.60$  and  $E_V + 2.67$  eV,

respectively. The (2+/0) transition level are located at  $E_V + 1.84$  eV [ $V_C(h)$ ] and  $E_V + 1.90$  eV [ $V_C(k)$ ]. It is well-known that the negative-U behavior does not occur to the charge transition level (+|0) of  $V_C$  at both inequivalent lattice sites.<sup>37,38</sup> In this calculation, the (+|0) level appears at  $V_C(h)$  but not at  $V_C(k)$ , which could contribute to the Coulomb interaction between the charged defects in different cells. However, this may not influence the formation energy of the calculated defects and the result is still valid.  $V_C^-$  and  $V_C^{2+}$  are the dominant types of  $V_C$  in *n*-type and *p*-type 4H-SiC, respectively. Therefore,  $(\text{Al}_i^{\text{C-te}})^{3+}$  and  $V_C^{2+}$  need to be the most seriously considered for the compensation of *p*-type doping in Al-doped SiC. Moreover, Al vacancy-complexes are also taken into consideration. For all the complexes,<sup>45,46</sup> except  $\text{Al}_{\text{Si}}-V_C$ , the formation energy of the complexes is high. It is reasonable only  $\text{Al}_{\text{Si}}-V_C$  complexes are involved.  $\text{Al}_{\text{Si}}-V_C$  are in 1+ and 3− charge states, and the (1+/3−) transition level is located at  $E_V + 2.61$  eV.

## B. Carrier density

Using the calculated defect formation energies and the detailed balance theory, we calculate the Fermi energies as well as the concentrations of holes and defects as functions of the chemical potential of  $\mu_C$ , which varies from point A to point C as shown in Fig. 1.  $\mu_{\text{Al}}$  is set as the highest value in its accessible region. Since the growth temperature of 4H-SiC substrate is around 2400 K, we take this temperature to investigate the compensation in 4H-SiC together with the room temperature of 300 K.

At 2400 K, the value of  $N_V$  is  $1.6 \times 10^{21} \text{ cm}^{-3}$ . Because the solubility of Al (from  $4.5 \times 10^{20}$  to  $7.2 \times 10^{20} \text{ cm}^{-3}$  as  $\mu_C$  varies from point A to point C) is less than  $N_V$  [Fig. 3(a)], we use the Boltzmann distribution to calculate the concentration of charged  $\text{Al}_{\text{Si}}$ . At 2400 K, the Fermi energy of 4H-SiC decreases from 0.69 to 0.46 eV with the increase of  $\mu_C$  because of the decreased  $\mu_{\text{Si}}$  that facilitates the formation of  $\text{Al}_{\text{Si}}$  acceptor. This indicates that the *p*-type doping of 4H-SiC can be enhanced by tuning the growth condition toward the C-rich condition. With the increase of  $\mu_C$ , the hole concentration increases from  $5.8 \times 10^{19}$  to  $1.8 \times 10^{20} \text{ cm}^{-3}$  [Fig. 3(a)]. The concentration of  $\text{Al}_{\text{Si}}^-$  is higher than that of holes by one order of magnitude, indicating that part of  $\text{Al}_{\text{Si}}^-$  is significantly compensated by intrinsic defects or is self-compensated. As shown in the bottom panel of Fig. 3(a), the calculated concentration of  $V_C^{2+}$  is as high as  $2 \times 10^{20} \text{ cm}^{-3}$  and the concentration of  $(\text{Al}_{\text{Si}}-V_C)^{1+}$  is  $5 \times 10^{19} \text{ cm}^{-3}$ , while the concentration of  $\text{Al}_i^{3+}$  is  $\sim 1.0 \times 10^{18} \text{ cm}^{-3}$ . Therefore, it is the dominant compensation of  $V_C^{2+}$  and supplementary self-compensation of  $\text{Al}_i^{3+}$  that give rise to the limited hole concentration of Al in 4H-SiC. For example, under the Si-rich limit, the concentration of  $\text{Al}_{\text{Si}}^-$  is  $5.4 \times 10^{20} \text{ cm}^{-3}$ , while the concentrations of  $V_C^{2+}$ ,  $(\text{Al}_{\text{Si}}-V_C)^{1+}$ , and  $\text{Al}_i^{3+}$  are  $1.6 \times 10^{20}$ ,  $5.4 \times 10^{19}$ , and  $1.0 \times 10^{18} \text{ cm}^{-3}$ , respectively. This means that in this case,  $\sim 30.0\%$  ( $(N_{V_C^{2+}} + N_{(\text{Al}_{\text{Si}}-V_C)^{1+}})/N_{\text{Al}_{\text{Si}}^-}$ ) of  $\text{Al}_{\text{Si}}^-$  is compensated by  $V_C^{2+}$ , while  $\sim 0.1\%$  ( $N_{\text{Al}_i^{3+}}/N_{\text{Al}_{\text{Si}}^-}$ ) of  $\text{Al}_{\text{Si}}^-$  is compensated by  $\text{Al}_i^{3+}$ .

When 4H-SiC is slowly cooled down to 300 K, the defect configurations and charge states have enough time to relax. Therefore, the concentrations of different defect configurations and charge states fully redistribute with the change of temperature. As 4H-SiC slowly cools down to 300 K, the amount of Al beyond the solution limit at 300 K will precipitate out. Eventually, At 300 K, the amount

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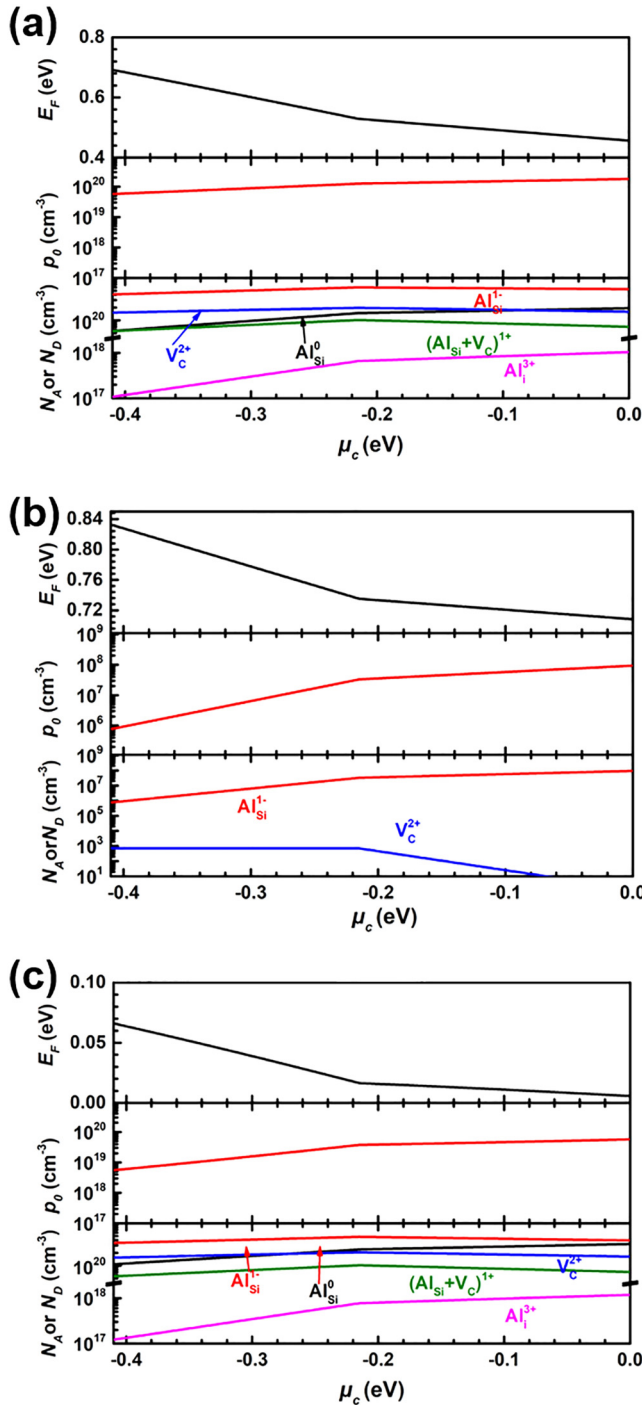


FIG. 3. Fermi energies ( $E_F$ ), hole concentrations ( $p_0$ ), and defect concentrations ( $N_A$  or  $N_D$ ) of Al-doped 4H-SiC as functions of  $\mu_C$ . (a) 4H-SiC is at the growth temperature of 2400 K. (b) 4H-SiC is slowly cooled down to the room temperature of 300 K. (c) 4H-SiC is quenched to the room temperature of 300 K.

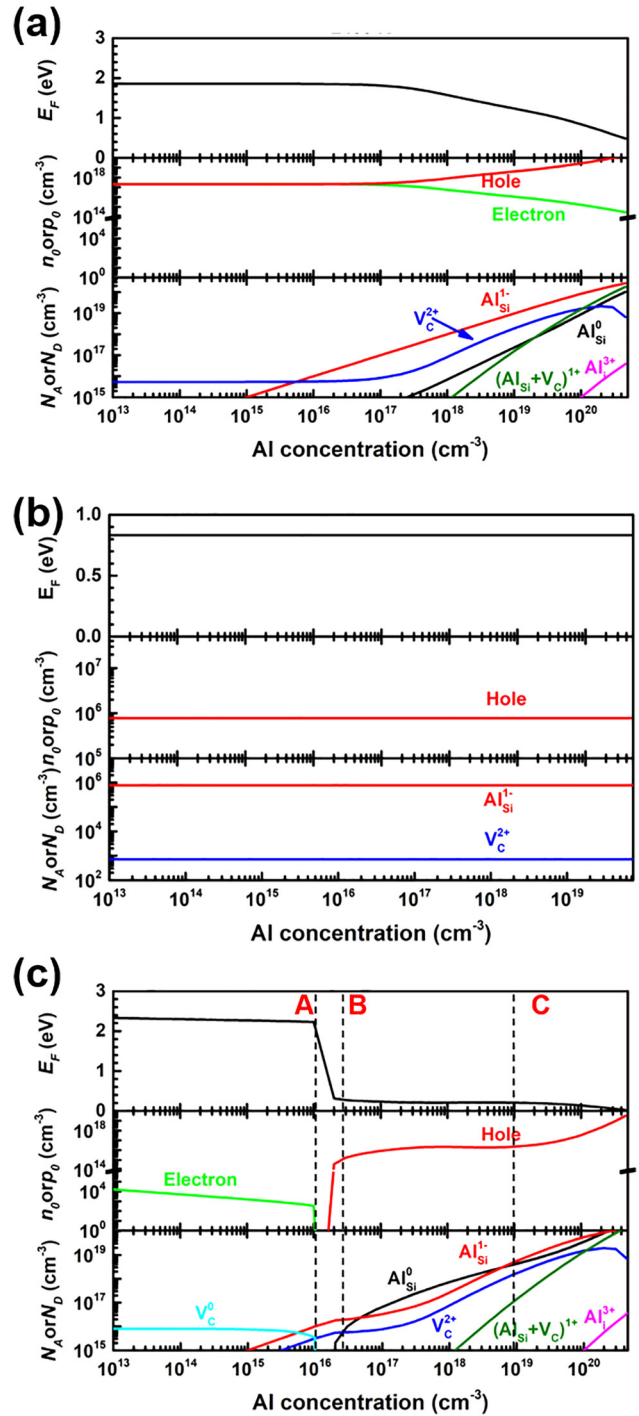


FIG. 4. Calculated Fermi energies ( $E_F$ ), electron or hole densities ( $n_0$  or  $p_0$ ), and defect concentrations ( $N_A$  or  $N_D$ ) of Al-doped 4H-SiC as functions of the concentration of Al. (a) 4H-SiC is at the growth temperature of 2400 K. (b) 4H-SiC is slowly cooled down to the room temperature of 300 K. (c) 4H-SiC is quenched to the room temperature of 300 K.

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of Al still occupied on the Si lattice ( $\text{Al}_{\text{Si}}$ ) is in the range of  $7.8 \times 10^5$  to  $9.3 \times 10^7 \text{ cm}^{-3}$  as  $\mu_{\text{C}}$  varies from point A to point C. As shown in Fig. 3(b),  $\text{Al}_{\text{Si}}$  is in the  $\text{Al}_{\text{Si}}^-$  charge state and  $\text{V}_{\text{C}}$  is in the dominant  $\text{V}_{\text{C}}^{2+}$  charge state. The concentrations of  $\text{Al}_{\text{Si}}^-$  and  $\text{V}_{\text{C}}^{2+}$  decrease to be lower than  $10^8 \text{ cm}^{-3}$ . The thermally excited holes make the pinned Fermi energy of 4H-SiC change from 0.83 to 0.70 eV when the growth condition changes from the Si-rich limit to the C-rich limit [as shown in Fig. 3(b)].

When 4H-SiC is rapidly quenched to 300 K, the total concentrations of defects are assumed to remain unchanged, while the concentrations of defects at different charge states redistribute according to their weights.<sup>47–50</sup> The concentrations of thermally excited electrons and holes decrease due to the decreased temperature. At lower temperatures, the concentration of  $\text{Al}_{\text{Si}}^-$  becomes larger than the effective densities of states of the valence bands ( $N_{\text{V}}$ ). Therefore, when 4H-SiC is rapidly quenched to 300 K, a degenerate *p*-type 4H-SiC is formed. The ionization energy [ $\epsilon(0/-)$ ] of Al decreases. We have used the Fermi–Dirac distribution to calculate the concentration of  $\text{Al}_{\text{Si}}^-$ . As shown in Fig. 3(c), when 4H-SiC is quenched from 2400 to 300 K, the concentrations of  $\text{Al}_{\text{Si}}^-$ ,  $\text{Al}_{\text{Si}}^{3+}$ ,  $(\text{Al}_{\text{Si}}-\text{V}_{\text{C}})^{1+}$ , and  $\text{V}_{\text{C}}^{2+}$  in 4H-SiC do not change significantly, giving rise to the decrease of the Fermi energy. This indicates that the *p*-type doping of SiC can be enhanced by quenching.

For Al-doped 4H-SiC at the growth temperature of 2400 K,  $\text{V}_{\text{C}}^{2+}$  is the dominant intrinsic defect. When the concentration of Al increases to the value larger than  $10^{16} \text{ cm}^{-3}$ , i.e., the concentration of  $\text{Al}_{\text{Si}}^-$  is larger than the  $\text{V}_{\text{C}}^{2+}$ , the Fermi energy of SiC begins to decrease. With the decrease of the Fermi energy, the concentration of  $\text{V}_{\text{C}}^{2+}$  rapidly increases, which gives rise to the compensation of *p*-type doping in Al-doped 4H-SiC. Even if the concentration of Al increases to  $4.5 \times 10^{20} \text{ cm}^{-3}$ , the Fermi energy of 4H-SiC is as high as 0.69 eV [Fig. 4(a)]. When 4H-SiC is slowly cooled down to 300 K because the doped concentration of Al at 2400 K exceeds the solid solubility limit ( $7.8 \times 10^5 \text{ cm}^{-3}$ ) at 300 K, the excess Al will precipitate out and the concentration keeps at  $7.8 \times 10^5 \text{ cm}^{-3}$ . The Fermi energy is stabilized at 0.83 eV, while the concentration of  $\text{Al}_{\text{Si}}^-$  is  $7.8 \times 10^5 \text{ cm}^{-3}$  and  $\text{V}_{\text{C}}^{2+}$  is  $7.1 \times 10^2 \text{ cm}^{-3}$  [Fig. 4(b)].

When 4H-SiC is rapidly quenched to 300 K, even with the effective compensation of  $\text{V}_{\text{C}}^{2+}$ , the Fermi energy decreases sharply due to the charge redistribution [Fig. 4(c)]. For 4H-SiC with the concentration of Al smaller than  $10^{16} \text{ cm}^{-3}$ , the thermally excited carriers pin the Fermi energy at  $\sim 2.3$  eV. In this case, the concentration of  $\text{Al}_{\text{Si}}^-$  is twice as large as that of  $\text{V}_{\text{C}}^{2+}$ , indicating that the holes of ionized  $\text{Al}_{\text{Si}}^-$  are totally compensated by  $\text{V}_{\text{C}}^{2+}$ . Once the concentration of Al increases to the value larger than the sum of  $\text{V}_{\text{C}}$  [point A as shown in Fig. 4(c)], the Fermi energy begins to decrease rapidly with the increase of the Al concentration. As the Al concentration increases from  $1.0 \times 10^{16}$  to  $2.0 \times 10^{16} \text{ cm}^{-3}$  (point A to point B as shown in Fig. 4),  $\text{Al}_{\text{Si}}^-$  is the dominant configuration of Al in 4H-SiC. The concentration of  $\text{Al}_{\text{Si}}^-$  becomes larger than the double of  $\text{V}_{\text{C}}^{2+}$ . This gives rise to the decrease of Fermi energy when the Al concentration increases from  $1.0 \times 10^{16}$  to  $2.0 \times 10^{16} \text{ cm}^{-3}$  [point A as shown in Fig. 4(c)] to  $2.0 \times 10^{16} \text{ cm}^{-3}$  [point B as shown in Fig. 4(c)]. As the Al concentration further increases from  $2.0 \times 10^{16} \text{ cm}^{-3}$  [point B as shown in Fig. 4(c)] to  $5.5 \times 10^{18} \text{ cm}^{-3}$  [point C as shown in Fig. 4(c)], the charge redistribution of  $\text{Al}_{\text{Si}}$

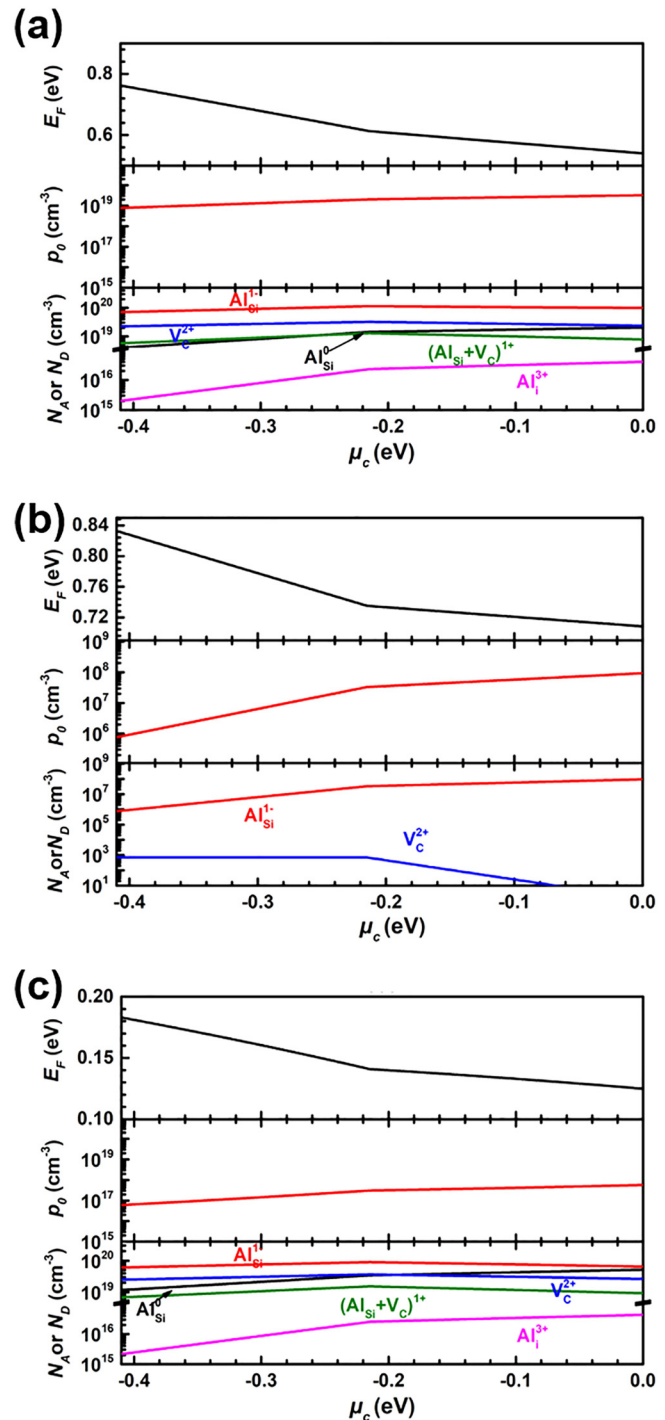
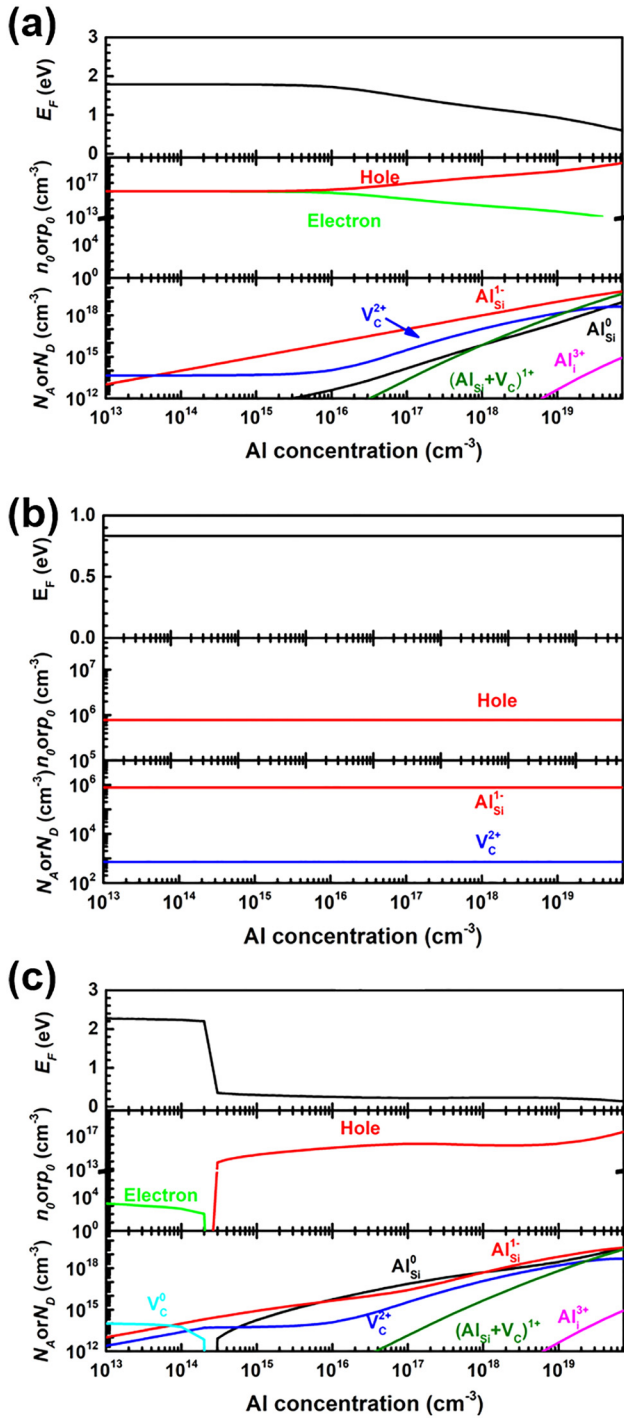


FIG. 5. Calculated Fermi energies ( $E_F$ ), hole densities ( $\rho_0$ ), and defect concentrations ( $N_A$  or  $N_D$ ) of Al-doped 4H-SiC as functions of  $\mu_{\text{C}}$ . (a) SiC is at the growth temperature of 1800 K. (b) SiC is slowly cooled down to the working temperature of 300 K. (c) SiC is quenched to the room temperature of 300 K.

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**FIG. 6.** Calculated Fermi energies ( $E_F$ ), hole densities ( $p_0$ ), and defect concentrations ( $N_A$  or  $N_D$ ) of Al-doped 4H-SiC as functions of the concentration of Al. (a) SiC is at the growth temperature of 1800 K. (b) SiC is slowly cooled down to the working temperature of 300 K. (c) SiC is quenched to the room temperature of 300 K.

leads to the increase of the concentration of  $Al_{Si}^0$ . The concentration of  $Al_{Si}^0$  becomes larger than  $Al_{Si}^-$ , but the concentration of  $Al_{Si}^-$  is still larger than that of  $V_C^{2+}$ . Therefore, the Fermi energy still decreases with the increase of the concentration of Al. When the concentration of Al exceeds  $5.5 \times 10^{18} \text{ cm}^{-3}$ , the ionization energy  $[\epsilon(0/-)]$  of Al sharply decreases, as shown in Fig. S1 in the [supplementary material](#). This leads to the higher ionization rate of  $Al_{Si}^-$ . The concentration of  $Al_{Si}^-$  becomes larger than  $Al_{Si}^0$ . As the concentration of Al reaches  $4.5 \times 10^{20} \text{ cm}^{-3}$ , the Fermi energy of 4H-SiC decreases to 0.14 eV if quenching takes place. It should be noted that even the compensation of  $V_C^{2+}$  plays an important role on the  $p$ -type doping of 4H-SiC with the Al concentration in the range from  $1.0 \times 10^{16}$  to  $4.5 \times 10^{20} \text{ cm}^{-3}$ ; quenching holds the potential of enhancing the  $p$ -type doping in Al-doped 4H-SiC.

We have also studied the Fermi energies, electron/hole concentrations, and defect concentrations as functions of the chemical potential (the concentration of Al) at the temperature of 1800 K and for quenching from 1800 to 300 K because the epitaxial growth temperature of 4H-SiC is around 1800 K. The results are shown in [Figs. 5 and 6](#). The dominant compensation of  $V_C^{2+}$  is also found. The Fermi energy of 4H-SiC grown at 1800 K is lower than that of 4H-SiC grown at 2400 K, as a result of the decreased concentration of ionized  $Al_{Si}$  at a lower temperature.

We now take 4H-SiC substrate (epilayer) grown at 2400 K (1800 K) under the Si-rich condition (point A in [Fig. 1](#)) and its use at 300 K as an example to evaluate the hole concentration of Al in 4H-SiC. For the 4H-SiC substrate (epilayer), the solubility limit of Al is  $4.5 \times 10^{20} \text{ cm}^{-3}$  ( $7.3 \times 10^{19} \text{ cm}^{-3}$ ). The calculated hole concentration of the 4H-SiC substrate (epilayer) is  $7.8 \times 10^{19} \text{ cm}^{-3}$  ( $6.1 \times 10^{18} \text{ cm}^{-3}$ ). The mobility of holes ( $\mu_p$ ) of the 4H-SiC substrate (epilayer) is  $2.8 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  ( $9.3 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ), which is obtained by using<sup>1</sup>

$$\mu_p = \frac{118}{1 + [(N_A + N_D)/2.2 \times 10^{18}]^{0.7}}. \quad (13)$$

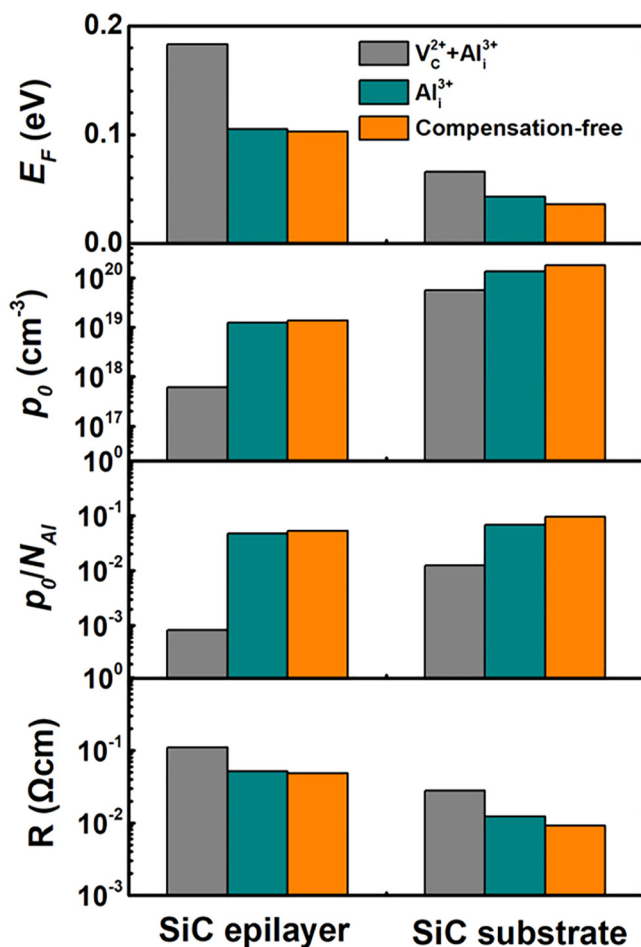
The resistivity of the 4H-SiC substrate (epilayer) is then 0.028  $\Omega \text{ cm}$  (0.11  $\Omega \text{ cm}$ ). Compared with the 4H-SiC substrate from solution growth, the calculated resistivity of the 4H-SiC substrate is in the same order of magnitude.<sup>24,25</sup> However, as for the epilayer, there exists a large difference between the calculated value and the experimental value. This is because dopant incorporation during epitaxial growth is kinetic controlled and solubility limits may be exceeded.<sup>51,52</sup> The Al doping concentration can reach up to  $\sim 5 \times 10^{20} \text{ cm}^{-3}$  with a resistance of  $\sim 0.016 \text{ } \Omega \text{ cm}$ .<sup>53,54</sup> Moreover, the compensation effect of  $V_C$  is very low and its compensation effect on Al can be mostly ignored. It found that the concentration of compensating defects in Al-doped 4H-SiC epilayers is very low (only <1% of the Al concentration).<sup>27,55</sup> This is because that the concentration of  $V_C$  of 4H-SiC epilayers is strongly dependent on the C/Si ratio and growth temperature. Through adjusting the C/Si ratio and growth temperature, the concentration of  $V_C$  can be controlled in a low level.<sup>56</sup>

Since the resistivity of 4H-SiC is mainly limited by the compensation of  $V_C^{2+}$ , the passivation of  $V_C^{2+}$  is highly desired to enhance the hole concentration of 4H-SiC. We may evaluate the possible improvement of the hole concentration of Al in 4H-SiC if

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$V_C$  is properly passivated. For the SiC substrate (epilayer) with the Al concentration reaching the solubility limit of  $4.5 \times 10^{20} \text{ cm}^{-3}$  ( $7.3 \times 10^{19} \text{ cm}^{-3}$ ), the Fermi energy is pinned at 0.06 eV (0.18 eV) due to the compensation of  $V_C^{2+}$  even if rapid quenching is used. If  $V_C$  is properly passivated, however, the Fermi energy decreases to 0.04 eV (0.1 eV) [Fig. 7]. With this passivation of  $V_C$ , the hole concentration of Al in 4H-SiC substrate (epilayer) increases from 1.24% (0.1%) to 6.82% (4.8%). By combining the passivation of  $V_C$  and quenching approach, the resistivity of the 4H-SiC substrate (epilayer) may decrease to 12 m $\Omega$  cm (51 m $\Omega$  cm). If the compensation of  $Al_i^{3+}$  is additionally removed, the hole concentration of Al in the 4H-SiC substrate (epilayer) increases to 9.6% (5.3%). The resistivity of the 4H-SiC substrate (epilayer) further decreases to 9 m $\Omega$  cm (48 m $\Omega$  cm).



**FIG. 7.** Comparison of Fermi energies ( $E_F$ ), hole densities ( $\rho_0$ ), doping efficiencies ( $\rho_0/N_{Al}$ ), and resistivities ( $R$ ) of Al doping SiC with the compensation of both  $V_C^{2+}$  and self-compensation ( $V_C^{2+} + Al_i^{3+}$ ), with only self-compensation ( $Al_i^{3+}$ ), and without any compensating centers (compensation-free).

#### IV. CONCLUSION

In conclusion, we have systematically investigated the compensation of native defects and self-compensation in Al-doped 4H-SiC. It has been found that  $V_C^{2+}$  are the dominant compensating centers in Al-doped 4H-SiC. When the concentration is in the range of  $10^{16}$ – $10^{19} \text{ cm}^{-3}$ , the concentration of holes is lower by one order of magnitude than the Al concentration because of the compensation of  $V_C^{2+}$ . As the Al concentration exceeds  $10^{20} \text{ cm}^{-3}$ , the concentration of holes is only in the order of magnitude of  $10^{19} \text{ cm}^{-3}$  owing to the dominant compensation of  $V_C^{2+}$  and supplementary self-compensation of  $Al_i^{3+}$ . The current work on the elucidation of the compensation of  $p$ -type doping in 4H-SiC should encourage the development of practical methods to remove the compensation of  $V_C^{2+}$  and quench 4H-SiC, realizing Al-doped 4H-SiC with very low resistivity.

#### SUPPLEMENTARY MATERIAL

See the [supplementary material](#) for Figs. S1 and S2.

#### ACKNOWLEDGMENTS

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#### AUTHOR DECLARATIONS

##### Conflict of Interest

The authors have no conflicts to disclose.

#### DATA AVAILABILITY

The data that support the findings of this study are available within the article and its [supplementary material](#).

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