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**Theoretical consideration of step-flow and two-dimensional**  ${\sf nucleation}$  modes in homoepitaxial growth of  $4H\text{-}{\rm SiC}$  on **(0001) vicinal surfaces under silicon-rich condition** 

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## **[Theoretical consideration of step-flow and two-dimensional nucleation](http://dx.doi.org/10.1063/1.3043433) [modes in homoepitaxial growth of 4](http://dx.doi.org/10.1063/1.3043433)H-SiC on**  $(0001)$  **vicinal surfaces under [silicon-rich condition](http://dx.doi.org/10.1063/1.3043433)**

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Reported experimental results on homoepitaxial growth of 4H-SiC on (0001) Si-face vicinal surfaces under silicon-rich conditions in a  $SiH_4 - C_3H_8 - H_2$  system are quantitatively analyzed according to the surface-diffusion theory dealing with step dynamics. The surface-diffusion length of  $C_2H_2$  molecules, which are the main carbon-containing chemical species reacting with silicon adatoms on the surface, is determined to be  $12-36$  nm at  $1500$  °C. According to the two-dimensional nucleation theory using these values, the maximum growth rate for step-flow growth is estimated as a function of the off-angle of 4*H*-SiC substrates. © *2008 American Institute of Physics*. DOI: [10.1063/1.3043433](http://dx.doi.org/10.1063/1.3043433)

Despite its polytypism, silicon carbide (SiC) has shown significant promise for high-power device applications.<sup>1</sup> This is due to homoepitaxial growth on off-oriented (0001) substrates (with an off angle  $\theta$  larger than 1.5°),<sup>2-[4](#page-3-2)</sup> in which polytype control is achieved by step-flow growth. On the other hand, to eliminate the basal plane dislocation issue that has hampered the reliability of bipolar<sup>5</sup> and metal-oxidesemiconductor power devices, $6$  there has been growing interest in the growth of  $4H$ -SiC on nominal<sup>7</sup> and vicinal<sup>8[,9](#page-3-7)</sup> (0001) surfaces. Although an uncommon gas (methyltri-chlorosilane) was supplied in Ref. [7,](#page-3-5) a conventional  $SiH_4 - C_3H_8 - H_2$  growth system for vapor-phase epitaxy (VPE) of SiC also achieved good surface morphology on 4*H*-SiC (0001) vicinal surfaces when the C/Si ratio (*r* is the atomic ratio of carbon and silicon in supplied gases) is less than unity:  $r=0.5-0.75$  for  $\theta=1^\circ$ , growth temperature  $T_g$ =1500 °C, growth pressure,  $P_g$ =80 Torr,<sup>8</sup> and  $r=0.6$  for  $\theta$ =0.79°,  $T_g$ =1600 °C, and  $P_g$ =250 mbar.<sup>9</sup>

Homoepitaxial growth on vicinal (0001) surfaces was achieved by Powell *et al.*<sup>[10](#page-3-8)</sup> in 1991 for 6*H*-SiC with  $\theta$  as small as 0.1°. Their polytype control was attributed to the presence of surface disturbances (e.g., dislocations), not to the surface step density.<sup>10</sup> In recent studies on homoepitaxial growth of 4*H*-SiC, however, the step bunching was observed when  $r=1$  for  $\theta=1^{\circ}$  (Ref. [8](#page-3-6)) and  $r=0.6$  for  $\theta=0.42^{\circ}$ ,<sup>9</sup> which means the epitaxial growths in Refs. [8](#page-3-6) and [9](#page-3-7) were carried out in the step-flow mode.<sup>11</sup> During step-flow growth under silicon-rich conditions, almost all of the step edges are assumed to be occupied by silicon [Fig.  $1(a)$  $1(a)$ ], and they can accept no more silicon atoms until another carbon atom enters the step edges, as discussed by Nishinaga and Suzuki<sup>12</sup> with regards to molecular beam epitaxy (MBE) of GaAs under gallium-rich conditions.

<span id="page-1-0"></span>According to the simulation of surface mass fluxes in  $SiH_4 - C_3H_8 - H_2$  growth system, <sup>13,[14](#page-3-12)</sup> the surface reaction of silicon adatoms with  $C_2H_2$ ,

<span id="page-1-2"></span>
$$
Si + (1/2)C_2H_2 \leftrightarrow SiC + (1/2)H_2
$$
 (1)

is most active among the surface reactions involved, including other carbon-containing species such as  $C_2H_4$ , CH<sub>4</sub>, CH<sub>3</sub>,  $Si<sub>2</sub>C$ , and CH<sub>2</sub>. Based on the reaction in Eq. (1), Kimoto and Matsunami analyzed using the Burton–Cabrera–Frank<sup>15</sup> (BCF) theory, the surface diffusion of silicon adatoms under carbon-rich conditions. However, they have not discussed the case under silicon-rich conditions.<sup>16</sup>

The BCF theory dealing with step dynamics $15$  has been applied for MBE in order to discuss the surface diffusion of silicon adatoms,<sup>17[,18](#page-3-16)</sup> gallium adatoms,<sup>19</sup> and  $As<sub>i</sub>$  and  $Sb<sub>i</sub>$  molecules  $(i=1, 2, \text{ and } 4)$ .<sup>[20](#page-3-18)</sup> Based mainly on the last approach by Mochizuki and Nishinaga, $^{20}$  the present study deals with surface diffusion of  $C_2H_2$  molecules during VPE growth on 4H-SiC (0001) Si-face vicinal surfaces under silicon-rich conditions.

<span id="page-1-1"></span>

FIG. 1. Schematic of growing silicon-rich 4H-SiC (0001) Si-face vicinal surface showing (a) atomic arrangement (hydrogen-passivation effect ignored) and (b) surface diffusion of  $C_2H_2$  molecules, and (c) distributions of supersaturation ratio for step-flow (broken curve) and two-dimensional nucleation modes (solid curve).

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Figure  $1(b)$  $1(b)$  schematically illustrates the surface model, where Si–C bilayer steps with height *h* are separated by equal distance  $\lambda_o$ . It is known that SiC homoepitaxial growth on off-oriented (0001) substrates results in microscopic step bunching, which is peculiar to SiC polytypes. $\frac{11}{11}$  In the case of  $4H-SiC$ , two- and four-bilayer heights are dominant,  $\frac{11}{11}$  i.e., *h*=0.504 or 1.01 nm. The steps are assumed to act as a uniform sink for the diffusing silicon adatoms and  $C_2H_2$  molecules on the surface. As reported by Saito and Kimoto,<sup>8</sup> growth rate *R* is limited by the supply of carbon under silicon-rich conditions. This fact allows the assumption that the surface diffusion of  $C_2H_2$  molecules is a rate-limiting process.

<span id="page-2-0"></span>Two modes are known to exist in the epitaxial growth of 4*H*-SiC. The first is step-flow growth mode, where nucleation on terraces does not occur. Since the net flux of  $C_2H_2$ molecules onto the surface is equal to the diffusion flux toward steps, the continuity equation is<sup>15</sup>

$$
-D_{s}d^{2}n_{s}(x)/dx^{2} = J - n_{s}(x)/\tau_{s},
$$
\n(2)

<span id="page-2-4"></span>where  $D_s$  and  $n_s(x)$  are the surface diffusivity and the surface density of  $C_2H_2$  molecules, respectively, and *J* is the flux of  $C_2H_2$  molecules arriving at the surface. Under the boundary condition where  $n_s(x)$  takes its equilibrium value  $n_{so}$  at the step edges,  $19$  the solution of Eq. ([2](#page-2-0)) is given by

$$
n_s(x) = J\tau_s + (n_{so} - J\tau_s) \left[ \cosh(x/\lambda_s) / \cosh(\lambda_o/2\lambda_s) \right],\tag{3}
$$

where  $\tau_s$  and  $\lambda_s$   $\equiv (D_s \tau_s)^{1/2}$  are the mean residence time and the surface diffusion length of  $C_2H_2$  molecules, respectively. The flow of  $C_2H_2$  molecules in the *x* direction  $J_s(x)$  is obtained as

$$
J_s(x) = -D_s dn_s(x)/dx
$$
  
=  $\lambda_s (J - n_{so}/\tau_s) \sinh(x/\lambda_s)/\cosh(\lambda_o/2\lambda_s)$ . (4)

<span id="page-2-1"></span>The step velocity is calculated by considering  $C_2H_2$  molecules diffusing from both the left and right sides of the steps. Since two carbon atoms are provided by one  $C_2H_2$ molecule at the step edges,  $^{20}R$  is given by the product of the step velocity and tan  $\theta$  (i.e.,  $h/\lambda_o$ ) as follows:<sup>16</sup>

$$
R = (4h\lambda_s/n_o\lambda_o)(J - n_{so}/\tau_s)\tanh(\lambda_o/2\lambda_s),
$$
\n(5)

where  $n<sub>o</sub>$  is the density of sites of adsorbed  $C_2H_2$  molecules on the surface. When  $\lambda_s \gg \lambda_o/2$ , *R* becomes independent of  $\lambda_o$  [i.e.,  $(2h/n_o)(J-n_{so}/\tau_s)$ ]. Since, according to Ref. [8](#page-3-6) *R* depends little on  $\theta$  when  $\theta = 4^{\circ} - 45^{\circ}$  but decreases when  $\theta$  $= 1^\circ$ ,  $\lambda_s$  is estimated to be comparable to or less than  $h/(2 \tan 1^\circ)$  [ $h/(2 \tan 1^\circ) = 14.4$  nm for  $h=0.504$  nm and 28.9 nm for  $h=1.01$  nm. If  $n<sub>o</sub>$  is assumed to be equal to the density of silicon adatom sites on the surface  $(1.21)$  $\times 10^{15}$  $\times 10^{15}$  $\times 10^{15}$  cm<sup>-3</sup>), *J*−*n<sub>so</sub>*/ $\tau_s$  can be calculated from Eq. (5). As is clear from Fig. [2,](#page-2-2) when  $\lambda_s = 12-18$  nm in the case of *h*  $= 0.504$  nm and  $\lambda_s = 24 - 36$  nm in the case of  $h = 1.01$  nm, the least-squares fit of  $J - n_{so}/\tau_s$  for  $\theta = 1^\circ$  fits among those for  $\theta = 4^{\circ} - 45^{\circ}$ . This  $\lambda_s$  range agrees with the above estimated value (i.e., 14.4 and 28.9 nm).

The absolute values of the intercept with the vertical axes in Figs.  $2(a)$  $2(a)$  and  $2(b)$  give an equilibrium desorption flux of  $C_2H_2$  molecules  $(n_{so}/\tau_s)$  of  $(0.5-1.2)$  $\times 10^{14}$  cm<sup>-2</sup> s<sup>-1</sup>. This corresponds to the equilibrium vapor pressure of C<sub>2</sub>H<sub>2</sub> molecules  $(P_o)$  of  $(0.4-1.0) \times 10^{-4}$  Pa, which is obtained from Knudsen's equation, $^{20}$ 

<span id="page-2-2"></span>

FIG. 2. Dependences of  $J - n_{so}/\tau_s$  on C/Si ratio calculated from Eq. ([5](#page-2-1)) for a surface diffusion length of 12–36 nm. Data denoted by symbols are taken from Saito and Kimoto's experiments (see Ref. [8](#page-3-6)), where 4*H*-SiC was grown on  $4H$ -SiC (0001) substrates with an off-angle of  $1^{\circ} - 45^{\circ}$  in a SiH<sub>4</sub>  $(1.5-2.0 \text{ scm})$ -C<sub>3</sub>H<sub>8</sub>-H<sub>2</sub> (8.0 slm)-Ar (0.8 slm) system (sccm denotes standard cubic centimeters per minute and slm denotes standard liters per minute) at a growth pressure of 80 Torr and a growth temperature of 1500 °C. Solid lines and corresponding equations show the least-squares fit to the results for an off-angle of 1°.

<span id="page-2-3"></span>
$$
n_{so}/\tau_s = P_o/(2\pi m k_B T_g)^{1/2},\tag{6}
$$

where *m* is the mass of a  $C_2H_2$  molecule and  $k_B$  is Boltzmann's constant. In regard to MBE growth, since molecules can arrive at the growing surface without any barrier and their beam equivalent flux can be measured,  $20 n_{s0}/\tau_s$  can be obtained from Eq.  $(6)$  $(6)$  $(6)$ . In regard to VPE growth, however, *Po* is difficult to determine because of many related parameters. $^{21}$  The procedure described above is thus effective for estimating  $n_{so}/\tau_s$  for VPE.

Next, the second growth mode, i.e., two-dimensional nucleation on terraces, is considered. Supersaturation ratios  $\alpha_{\rm C}$  and  $\alpha_{\rm Si}$  are defined as  $n_s(x)/n_{so}$  for C<sub>2</sub>H<sub>2</sub> molecules and similarly for silicon adatoms, respectively. As mentioned above, under silicon-rich conditions, the equilibrium vapor pressure of silicon adatoms must be similar to the incoming pressure of silicon, i.e.,  $\alpha_{Si}$  nearly equals unity.<sup>19</sup> Since  $\alpha_C$ reaches a maximum at the center of a terrace, i.e.,  $x=0$  [Fig. [1](#page-1-1)(c)], the maximum supersaturation ratio for SiC is obtained from Eq.  $(3)$  $(3)$  $(3)$  as

<span id="page-2-5"></span>
$$
\alpha_{\text{max}} \equiv \alpha_{\text{Si}} \alpha_{\text{C}}(x=0) \approx 1 + (\lambda_o n_o R / 4h \lambda_s)
$$
  
 
$$
\times (\tau_s / n_{so}) \tanh(\lambda_o / 4\lambda_s). \tag{7}
$$

<span id="page-2-6"></span>Nucleation on terraces becomes dominant when  $\alpha_{\text{max}}$  exceeds  $\alpha_{\rm crit}$  [solid curve in Fig. [1](#page-1-1)(c)]. For a disk-shaped nucleation per second on a  $10\times10$  nm<sup>2</sup> area,  $\alpha_{\text{crit}}$  is given by<sup>19</sup>

$$
\alpha_{\rm crit} = \exp\{\pi h_1 \Omega \sigma^2 / [(65 - \ln 10^{12}) k_B^2 T_g^2] \},\tag{8}
$$

where  $h_1$  is the one Si–C bilayer height (0.252 nm),  $\Omega$  is the volume of the Si–C pair  $(2.07 \times 10^{-23} \text{ cm}^3)$ , and  $\sigma$  is the surface free energy, which is assumed to be 2.22  $J/m^2$ , as Kimoto and Matsunami<sup>16</sup> speculated from the calculation for  $3*C*-SiC (111) by Pearson *et al.*<sup>22</sup> From Eqs. (7) and (8), the$  $3*C*-SiC (111) by Pearson *et al.*<sup>22</sup> From Eqs. (7) and (8), the$  $3*C*-SiC (111) by Pearson *et al.*<sup>22</sup> From Eqs. (7) and (8), the$  $3*C*-SiC (111) by Pearson *et al.*<sup>22</sup> From Eqs. (7) and (8), the$  $3*C*-SiC (111) by Pearson *et al.*<sup>22</sup> From Eqs. (7) and (8), the$  $3*C*-SiC (111) by Pearson *et al.*<sup>22</sup> From Eqs. (7) and (8), the$  $3*C*-SiC (111) by Pearson *et al.*<sup>22</sup> From Eqs. (7) and (8), the$ 

<span id="page-3-21"></span>

FIG. 3. Off-angle dependences of critical growth rate for a mode transition between step-flow (bottom-right region) and two-dimensional nucleation (top-left region) calculated with three sets of two parameters, namely, equilibrium desorption flux and surface diffusion length of  $C_2H_2$  molecules, obtained from Fig. [2.](#page-2-2) Data denoted by symbols are taken from the experi-ment of Saito and Kimoto (see Ref. [8](#page-3-6)).

off-angle dependence of the critical growth rate  $(R_c)$  for mode transition between step-flow and two-dimensional nucleation is calculated at  $T<sub>g</sub> = 1500$  °C. As is clear from Fig. [3,](#page-3-21) the range of  $R<sub>C</sub>$ , originating from the variation in determining  $\lambda_s$  (Fig. [2](#page-2-2)), does not depend on *h* (*h*=0.504 or 1.01 nm). It is also confirmed that the three experimental data for step-flow growth in Ref. [8](#page-3-6) are in the bottom-right region under the curves calculated using the  $n_{so}/\tau_s$  and  $\lambda_s$  values obtained from Fig. [2.](#page-2-2)

As expected from Eq.  $(7)$  $(7)$  $(7)$ ,  $R_c$  increases with increasing  $n_{so}$  / $\tau_s$ . According to Eqs. ([1](#page-1-2)) and ([6](#page-2-3)), the increase in  $n_{so}$  / $\tau_s$ , i.e., the increase in  $P_o$ , is achieved by the reduction in the  $SiH<sub>4</sub>$  flow rate. However, to maintain *r* at less than unity (silicon-rich conditions), the  $C_3H_8$  flow rate has to be limited, resulting in lower  $R_c$ . The calculated curves in Fig. [3](#page-3-21) are thus considered to be close to the practical limit at  $T_g$ =1500 °C. To carry out a similar calculation at different  $T_g$ , e.g., 1600  $\degree$ C, <sup>9</sup> the dependence of *R* on *r* has to be experimentally determined because of the difficulty in estimating *Po* described above.

In summary, according to the surface diffusion and twodimensional nucleation theories, a surface diffusion length of  $C_2H_2$  molecules on  $4H\text{-SiC}$  (0001) was derived as 12–36 nm at 1500 °C in a  $SiH_4-C_3H_8-H_2$  system, and the maximum growth rate for step-flow growth was estimated as a function of the off-angle of 4*H*-SiC substrates.

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