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## Theoretical consideration of step-flow and two-dimensional nucleation modes in homoepitaxial growth of 4*H*-SiC on (0001) vicinal surfaces under silicon-rich condition

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Reported experimental results on homoepitaxial growth of 4*H*-SiC on (0001) Si-face vicinal surfaces under silicon-rich conditions in a SiH<sub>4</sub>-C<sub>3</sub>H<sub>8</sub>-H<sub>2</sub> system are quantitatively analyzed according to the surface-diffusion theory dealing with step dynamics. The surface-diffusion length of C<sub>2</sub>H<sub>2</sub> molecules, which are the main carbon-containing chemical species reacting with silicon adatoms on the surface, is determined to be 12–36 nm at 1500 °C. According to the two-dimensional nucleation theory using these values, the maximum growth rate for step-flow growth is estimated as a function of the off-angle of 4*H*-SiC substrates. © 2008 American Institute of Physics. [DOI: 10.1063/1.3043433]

Despite its polytypism, silicon carbide (SiC) has shown significant promise for high-power device applications.<sup>1</sup> This is due to homoepitaxial growth on off-oriented (0001) substrates (with an off angle  $\theta$  larger than 1.5°),<sup>2–4</sup> in which polytype control is achieved by step-flow growth. On the other hand, to eliminate the basal plane dislocation issue that has hampered the reliability of bipolar<sup>5</sup> and metal-oxidesemiconductor power devices,<sup>6</sup> there has been growing interest in the growth of 4H-SiC on nominal<sup>7</sup> and vicinal<sup>8,9</sup> (0001) surfaces. Although an uncommon gas (methyltrichlorosilane) was supplied in Ref. 7, a conventional  $SiH_4-C_3H_8-H_2$  growth system for vapor-phase epitaxy (VPE) of SiC also achieved good surface morphology on 4H-SiC (0001) vicinal surfaces when the C/Si ratio (r is the atomic ratio of carbon and silicon in supplied gases) is less than unity: r=0.5-0.75 for  $\theta=1^{\circ}$ , growth temperature  $T_g$ =1500 °C, growth pressure,  $P_g$ =80 Torr,<sup>8</sup> and r=0.6 for  $\theta$ =0.79°,  $T_g$ =1600 °C, and  $P_g$ =250 mbar.<sup>9</sup>

Homoepitaxial growth on vicinal (0001) surfaces was achieved by Powell *et al.*<sup>10</sup> in 1991 for 6*H*-SiC with  $\theta$  as small as 0.1°. Their polytype control was attributed to the presence of surface disturbances (e.g., dislocations), not to the surface step density.<sup>10</sup> In recent studies on homoepitaxial growth of 4*H*-SiC, however, the step bunching was observed when r=1 for  $\theta=1^{\circ}$  (Ref. 8) and r=0.6 for  $\theta=0.42^{\circ}$ ,<sup>9</sup> which means the epitaxial growths in Refs. 8 and 9 were carried out in the step-flow mode.<sup>11</sup> During step-flow growth under silicon-rich conditions, almost all of the step edges are assumed to be occupied by silicon [Fig. 1(a)], and they can accept no more silicon atoms until another carbon atom enters the step edges, as discussed by Nishinaga and Suzuki<sup>12</sup> with regards to molecular beam epitaxy (MBE) of GaAs under gallium-rich conditions.

According to the simulation of surface mass fluxes in  $SiH_4-C_3H_8-H_2$  growth system,<sup>13,14</sup> the surface reaction of silicon adatoms with  $C_2H_2$ ,

$$\operatorname{Si} + (1/2)\operatorname{C}_{2}\operatorname{H}_{2} \leftrightarrow \operatorname{SiC} + (1/2)\operatorname{H}_{2}$$
(1)

is most active among the surface reactions involved, including other carbon-containing species such as  $C_2H_4$ ,  $CH_4$ ,  $CH_3$ ,  $Si_2C$ , and  $CH_2$ . Based on the reaction in Eq. (1), Kimoto and Matsunami analyzed using the Burton–Cabrera–Frank<sup>15</sup> (BCF) theory, the surface diffusion of silicon adatoms under carbon-rich conditions. However, they have not discussed the case under silicon-rich conditions.<sup>16</sup>

The BCF theory dealing with step dynamics<sup>15</sup> has been applied for MBE in order to discuss the surface diffusion of silicon adatoms,<sup>17,18</sup> gallium adatoms,<sup>19</sup> and As<sub>i</sub> and Sb<sub>i</sub> molecules (i=1, 2, and 4).<sup>20</sup> Based mainly on the last approach by Mochizuki and Nishinaga,<sup>20</sup> the present study deals with surface diffusion of C<sub>2</sub>H<sub>2</sub> molecules during VPE growth on 4*H*-SiC (0001) Si-face vicinal surfaces under silicon-rich conditions.



FIG. 1. Schematic of growing silicon-rich 4*H*-SiC (0001) Si-face vicinal surface showing (a) atomic arrangement (hydrogen-passivation effect ignored) and (b) surface diffusion of  $C_2H_2$  molecules, and (c) distributions of supersaturation ratio for step-flow (broken curve) and two-dimensional nucleation modes (solid curve).

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Figure 1(b) schematically illustrates the surface model, where Si–C bilayer steps with height *h* are separated by equal distance  $\lambda_o$ . It is known that SiC homoepitaxial growth on off-oriented (0001) substrates results in microscopic step bunching, which is peculiar to SiC polytypes.<sup>11</sup> In the case of 4*H*-SiC, two- and four-bilayer heights are dominant,<sup>11</sup> i.e., *h*=0.504 or 1.01 nm. The steps are assumed to act as a uniform sink for the diffusing silicon adatoms and C<sub>2</sub>H<sub>2</sub> molecules on the surface. As reported by Saito and Kimoto,<sup>8</sup> growth rate *R* is limited by the supply of carbon under silicon-rich conditions. This fact allows the assumption that the surface diffusion of C<sub>2</sub>H<sub>2</sub> molecules is a rate-limiting process.

Two modes are known to exist in the epitaxial growth of 4H-SiC. The first is step-flow growth mode, where nucleation on terraces does not occur. Since the net flux of  $C_2H_2$  molecules onto the surface is equal to the diffusion flux toward steps, the continuity equation is<sup>15</sup>

$$-D_{s}d^{2}n_{s}(x)/dx^{2} = J - n_{s}(x)/\tau_{s},$$
(2)

where  $D_s$  and  $n_s(x)$  are the surface diffusivity and the surface density of C<sub>2</sub>H<sub>2</sub> molecules, respectively, and *J* is the flux of C<sub>2</sub>H<sub>2</sub> molecules arriving at the surface. Under the boundary condition where  $n_s(x)$  takes its equilibrium value  $n_{so}$  at the step edges,<sup>19</sup> the solution of Eq. (2) is given by

$$n_s(x) = J\tau_s + (n_{so} - J\tau_s)[\cosh(x/\lambda_s)/\cosh(\lambda_o/2\lambda_s)], \qquad (3)$$

where  $\tau_s$  and  $\lambda_s [\equiv (D_s \tau_s)^{1/2}]$  are the mean residence time and the surface diffusion length of C<sub>2</sub>H<sub>2</sub> molecules, respectively. The flow of C<sub>2</sub>H<sub>2</sub> molecules in the *x* direction  $J_s(x)$  is obtained as

$$J_{s}(x) = -D_{s}dn_{s}(x)/dx$$
  
=  $\lambda_{s}(J - n_{so}/\tau_{s})\sinh(x/\lambda_{s})/\cosh(\lambda_{o}/2\lambda_{s}).$  (4)

The step velocity is calculated by considering  $C_2H_2$  molecules diffusing from both the left and right sides of the steps. Since two carbon atoms are provided by one  $C_2H_2$  molecule at the step edges, <sup>20</sup> *R* is given by the product of the step velocity and tan  $\theta$  (i.e.,  $h/\lambda_o$ ) as follows:<sup>16</sup>

$$R = (4h\lambda_s/n_o\lambda_o)(J - n_{so}/\tau_s)\tanh(\lambda_o/2\lambda_s),$$
(5)

where  $n_o$  is the density of sites of adsorbed  $C_2H_2$  molecules on the surface. When  $\lambda_s \gg \lambda_o/2$ , *R* becomes independent of  $\lambda_o$  [i.e.,  $(2h/n_o)(J-n_{so}/\tau_s)$ ]. Since, according to Ref. 8 *R* depends little on  $\theta$  when  $\theta=4^\circ-45^\circ$  but decreases when  $\theta$ =1°,  $\lambda_s$  is estimated to be comparable to or less than  $h/(2 \tan 1^\circ)$  [ $h/(2 \tan 1^\circ)=14.4$  nm for h=0.504 nm and 28.9 nm for h=1.01 nm]. If  $n_o$  is assumed to be equal to the density of silicon adatom sites on the surface (1.21  $\times 10^{15}$  cm<sup>-3</sup>),  $J-n_{so}/\tau_s$  can be calculated from Eq. (5). As is clear from Fig. 2, when  $\lambda_s=12-18$  nm in the case of h=0.504 nm and  $\lambda_s=24-36$  nm in the case of h=1.01 nm, the least-squares fit of  $J-n_{so}/\tau_s$  for  $\theta=1^\circ$  fits among those for  $\theta=4^\circ-45^\circ$ . This  $\lambda_s$  range agrees with the above estimated value (i.e., 14.4 and 28.9 nm).

The absolute values of the intercept with the vertical axes in Figs. 2(a) and 2(b) give an equilibrium desorption flux of C<sub>2</sub>H<sub>2</sub> molecules  $(n_{so}/\tau_s)$  of  $(0.5-1.2) \times 10^{14}$  cm<sup>-2</sup> s<sup>-1</sup>. This corresponds to the equilibrium vapor pressure of C<sub>2</sub>H<sub>2</sub> molecules  $(P_o)$  of  $(0.4-1.0) \times 10^{-4}$  Pa, which is obtained from Knudsen's equation,<sup>20</sup>



FIG. 2. Dependences of  $J - n_{so}/\tau_s$  on C/Si ratio calculated from Eq. (5) for a surface diffusion length of 12–36 nm. Data denoted by symbols are taken from Saito and Kimoto's experiments (see Ref. 8), where 4*H*-SiC was grown on 4*H*-SiC (0001) substrates with an off-angle of 1°–45° in a SiH<sub>4</sub> (1.5–2.0 sccm)-C<sub>3</sub>H<sub>8</sub>–H<sub>2</sub> (8.0 slm)-Ar (0.8 slm) system (sccm denotes standard cubic centimeters per minute and slm denotes standard liters per minute) at a growth pressure of 80 Torr and a growth temperature of 1500 °C. Solid lines and corresponding equations show the least-squares fit to the results for an off-angle of 1°.

$$n_{so}/\tau_s = P_o/(2\pi m k_B T_g)^{1/2},$$
(6)

where *m* is the mass of a  $C_2H_2$  molecule and  $k_B$  is Boltzmann's constant. In regard to MBE growth, since molecules can arrive at the growing surface without any barrier and their beam equivalent flux can be measured,  ${}^{20} n_{so}/\tau_s$  can be obtained from Eq. (6). In regard to VPE growth, however,  $P_o$  is difficult to determine because of many related parameters.<sup>21</sup> The procedure described above is thus effective for estimating  $n_{so}/\tau_s$  for VPE.

Next, the second growth mode, i.e., two-dimensional nucleation on terraces, is considered. Supersaturation ratios  $\alpha_{\rm C}$  and  $\alpha_{\rm Si}$  are defined as  $n_s(x)/n_{so}$  for C<sub>2</sub>H<sub>2</sub> molecules and similarly for silicon adatoms, respectively. As mentioned above, under silicon-rich conditions, the equilibrium vapor pressure of silicon adatoms must be similar to the incoming pressure of silicon, i.e.,  $\alpha_{\rm Si}$  nearly equals unity.<sup>19</sup> Since  $\alpha_{\rm C}$  reaches a maximum at the center of a terrace, i.e., x=0 [Fig. 1(c)], the maximum supersaturation ratio for SiC is obtained from Eq. (3) as

$$\alpha_{\max} \equiv \alpha_{Si} \alpha_C (x=0) \approx 1 + (\lambda_o n_o R/4h\lambda_s) \\ \times (\tau_s/n_{so}) \tanh(\lambda_o/4\lambda_s).$$
(7)

Nucleation on terraces becomes dominant when  $\alpha_{\text{max}}$  exceeds  $\alpha_{\text{crit}}$  [solid curve in Fig. 1(c)]. For a disk-shaped nucleation per second on a 10×10 nm<sup>2</sup> area,  $\alpha_{\text{crit}}$  is given by<sup>19</sup>

$$\alpha_{\rm crit} = \exp\{\pi h_1 \Omega \sigma^2 / [(65 - \ln 10^{12}) k_B^2 T_g^2]\},\tag{8}$$

where  $h_1$  is the one Si–C bilayer height (0.252 nm),  $\Omega$  is the volume of the Si–C pair (2.07×10<sup>-23</sup> cm<sup>3</sup>), and  $\sigma$  is the surface free energy, which is assumed to be 2.22 J/m<sup>2</sup>, as Kimoto and Matsunami<sup>16</sup> speculated from the calculation for 3*C*-SiC (111) by Pearson *et al.*<sup>22</sup> From Eqs. (7) and (8), the



FIG. 3. Off-angle dependences of critical growth rate for a mode transition between step-flow (bottom-right region) and two-dimensional nucleation (top-left region) calculated with three sets of two parameters, namely, equilibrium desorption flux and surface diffusion length of  $C_2H_2$  molecules, obtained from Fig. 2. Data denoted by symbols are taken from the experiment of Saito and Kimoto (see Ref. 8).

off-angle dependence of the critical growth rate  $(R_c)$  for mode transition between step-flow and two-dimensional nucleation is calculated at  $T_g = 1500$  °C. As is clear from Fig. 3, the range of  $R_c$ , originating from the variation in determining  $\lambda_s$  (Fig. 2), does not depend on h (h=0.504 or 1.01 nm). It is also confirmed that the three experimental data for step-flow growth in Ref. 8 are in the bottom-right region under the curves calculated using the  $n_{so}/\tau_s$  and  $\lambda_s$  values obtained from Fig. 2.

As expected from Eq. (7),  $R_c$  increases with increasing  $n_{so}/\tau_s$ . According to Eqs. (1) and (6), the increase in  $n_{so}/\tau_s$ , i.e., the increase in  $P_o$ , is achieved by the reduction in the SiH<sub>4</sub> flow rate. However, to maintain r at less than unity (silicon-rich conditions), the C<sub>3</sub>H<sub>8</sub> flow rate has to be limited, resulting in lower  $R_c$ . The calculated curves in Fig. 3 are thus considered to be close to the practical limit at  $T_g$  = 1500 °C. To carry out a similar calculation at different  $T_g$ , e.g., 1600 °C, <sup>9</sup> the dependence of R on r has to be experimentally determined because of the difficulty in estimating  $P_o$  described above.

In summary, according to the surface diffusion and twodimensional nucleation theories, a surface diffusion length of  $C_2H_2$  molecules on 4*H*-SiC (0001) was derived as 12–36 nm at 1500 °C in a SiH<sub>4</sub>– $C_3H_8$ – $H_2$  system, and the maximum growth rate for step-flow growth was estimated as a function of the off-angle of 4*H*-SiC substrates.

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